

Recitation Guide - Week 12

Topics Covered: Probabilistic Method

Problem 1:

Let G be a bipartite graph with $|V| = n$. Suppose you give each vertex its own list of more than $\log_2 n$ possible colors.

Show that it is possible to provide a valid coloring of G choosing each vertex's color from its own list

Problem 2:

Given an arbitrary graph $G(V, E)$, show that there exists an independent set of size at least:

$$\sum_{v \in V} \frac{1}{\deg(v) + 1}$$