Zero Sum Games and the Minimax Thoerem

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- ▶ They have a very special property: the minimax theorem.
- ► And a close connection to the polynomial weights algorithm (and related algorithms)
- ▶ Playing the polynomial weights algorithm in a zero sum game leads to equilibrium (a plausible dynamic!)
- ▶ In fact, we'll use it to prove the minimax theorem.

Zero Sum Games

Definition

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- 1. Strictly adversarial games: The only way for player 1 to improve his payoff is to harm player 2, and vice versa.
- 2. Closely related to linear programming, adversarial machine learning, and lots of other things.

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The row player (Max) wishes to *maximize* the utility. The column player (Min) wishes to *minimize* the utility.

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- 3. Min should pick the action that minimizes her cost! She can compute:

$$\mathrm{E[Morality]} = \frac{1}{2} \cdot 3 + \frac{1}{2} \cdot (-2) = \frac{1}{2}$$

$$E[Tax - Cuts] = \frac{1}{2} \cdot (-1) + \frac{1}{2} \cdot 1 = 0$$

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4. So she plays Tax-cuts.



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5. And if Min goes first, she should play:

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- 5. And when Min best responds, he gets payoff 1 2p = 1/7.



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- 4. Lets investigate further...

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Definition

For an $n \times m$ matrix U (think about this as the payoff matrix in a two player zero sum game if you like):

$$\max \min(U) = \max_{p \in \Delta[n]} \min_{y \in [m]} \sum_{i=1}^{n} p_i \cdot U(i, y)$$

$$\min \max(U) = \min_{q \in \Delta[m]} \max_{x \in [n]} \sum_{i=1}^{m} q_j \cdot U(x, j)$$

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If U is a zero sum game, then $\max \min(U)$ represents the payoff that Max can guarantee if he goes first, and $\min \max(U)$ represents the payoff that he can guarantee if Min goes first.

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All Nash equilibria in Zero sum games have the same payoff — the max min value of the game.

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- 4. Previously, Borell had proven it for the special case of 5×5 matrices, and thought it was false for larger matrices.
- 5. But well give an easy, constructive proof.

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Proof

- 1. Suppose the theorem were false: there is some game U for which min $\max(U) > \max\min(U)$.
- 2. Write $v_1 = \min \max(U)$ and $v_2 = \max \min(U)$ (And so $v_1 = v_2 + \epsilon$ for some constant $\epsilon > 0$).
- 3. In other words: if Min has to go first, then Max can guarantee payoff at least v_1 , but if Max is forced to go first, then Min can force Max to have payoff only v_2 .

Lets consider what happens when Min and Max repeatedly play against each other as follows, for $\mathcal T$ rounds:

- Min will play using the polynomial weights algorithm. i.e. at each round t, the weights w^t of the polynomial weights algorithm will form her mixed strategy, and she will sample an action at random from this distribution, updating based on the losses she experiences at that round.
- 2. Max will play the best response to Min's strategy. i.e. Max will play $x^t = \arg\max_x \mathrm{E}_{y \sim w^t}[U(x,y)]$.

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What we know about each player's average payoffs when they play in this manner?

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By definition, $\min_{y^*} \mathrm{E}_{x \sim \bar{x}} U(x, y^*) \leq \max \min(U) = v_2$ and so:

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Taking T large enough leads to contradiction.



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- 3. It does so without needing to know what the game is. The game matrix is not an input to the PW algorithm!
- 4. The only information needed is the realized payoffs are for the actions as it plays the game.

Thanks!

See you next class — stay healthy!